

VPython: Ball bouncing around a box

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Getting started

Sign in at <http://glowscript.org>, then click to go to your program space (click on your username in top left or top right).

Click **Create New Program** and choose a name for your program (maybe 'BoxedBall'). Note that any spaces and underscores will be deleted from the name. You will see a blank edit window.

As the second line of the program, type

```
sphere()
```

Now click **Run this program**

Click **Edit this program** to return to the edit window. The goal of the activity is to make a ball which bounces around a box, in 3D. You will use the velocity to update the position, to create a 3D animation.

Adapt your program by writing

```
ball = sphere(pos=vector(-5,0,0), radius=0.5, color=color.cyan)
wallR = box(pos=vector(6,0,0), size=vector(0.2,12,12), color=color.green)
```

(There are 9 default colors: red green blue yellow magenta cyan orange black white—you can also design your own colours.)

Updating Position

We are going to make the ball move across the screen and bounce off of the wall. We can think of this as displaying 'snapshots' of the position of the ball at successive times as it moves across the screen. To specify how far the ball moves, we need to specify its velocity and how much time has elapsed.

We need to specify the velocity of the ball. We can make the velocity of the ball an attribute of the ball, by calling it `ball.velocity`. Since the ball can move in three dimensions, we must specify the x , y , and z components of the ball's velocity. We do this by making `ball.velocity` a vector. Add this statement to your program:

```
ball.velocity = vector(25,0,0)
```

We need to specify a time interval between ‘snapshots’. We’ll call this very short time interval `deltat`. To keep track of how much total time has elapsed, let’s also set a ‘stopwatch’ time to start from zero. Add these statements to your program:

```
deltat = 0.005
t = 0
```

If you run the program, nothing will happen, because we have not yet given instructions on how to update the ball’s position between snapshots. We need to use the velocity to move us from the initial position to give us the final position: the final (vector) position is the initial position plus the average velocity times the time interval,

$$\mathbf{r}_{\text{final}} = \mathbf{r}_{\text{initial}} + \mathbf{v}t.$$

This ‘position update’ relationship is valid if the velocity is nearly constant (both magnitude and direction) during the short time interval. If the velocity is changing (in magnitude and/or direction), you need to use a short enough time interval that the velocity at the start of the time interval is nearly the same as the average velocity during the whole time interval.

```
ball.pos = ball.pos + ball.velocity * deltat
```

Just as velocity is a vector, so is the position of the ball, `ball.pos`. As in most programming languages, the equals sign means something different than it does in ordinary algebra notation. In VPython, the equals sign is used for assignment, not equality. That is, the statement assigns the vector `ball.pos` a new value, which is the current value of `ball.pos` plus the displacement `ball.velocity * deltat`, the change in the position.

3D animation

Your program should now look like this:

```
1 GlowScript 1.1 VPython
2
3 ball = sphere(pos=vector(-5,0,0), radius=0.5, color=color.cyan)
4 wallR = box(pos=vector(6,0,0), size=vector(0.2,12,12), color=color.green)
5
6 ball.velocity = vector(25,0,0)
7 deltat = 0.005
8 t = 0
9
10 ball.pos = ball.pos + ball.velocity * deltat
```



If you run this, not much happens! The problem is that the program only took one time step; we need to take many steps. To accomplish this, we write a while loop. A while loop instructs the computer to keep executing a series of commands over and over again, until we tell it to stop.

Insert the following line just before your position update statement (that is, just before the last statement)

```
while t < 3:
```

Don't forget the colon! Notice that when you press return, the cursor appears at an indented location after the while statement. The indented lines following a while statement are inside the loop; that is, they will be repeated over and over. In this case, they will be repeated as long as the 'stopwatch' time `t` is less than 3 seconds. Indent your position update statement under the while statement

```
while t < 3:
    ball.pos = ball.pos + ball.velocity * deltat
```

Note that if you position your cursor at the end of the while statement, the text editor will automatically indent the next lines when you press  (ENTER). Alternatively, you can press  (TAB) to indent a line. All indented statements after a while statement will be executed every time the loop is executed.

Also update the stopwatch time by adding `deltat` to `t` for each passage through the loop:

```
t = t + deltat
```

Run your program. Because computers are very fast, the ball moved so fast that you saw only a flash! Moreover, VPython by default tries to keep all of the objects visible, so as the ball moves far away from the origin, VPython moves the 'camera' back, and the wall recedes into the distance. This is called 'autoscaling'. To slow down the animation, insert the following statement inside the loop (just after the while statement, indented as usual):

```
rate(100)
```



This specifies that the while loop will not be executed more than 100 times per second, even if your computer is capable of many more than 100 loops per second. (The way it works is that each time around the loop VPython checks to see whether 1/100 second has elapsed since the previous iteration. If not, VPython waits until that much time has gone by. This ensures that there are no more than 100 iterations performed in one second.)

Run your program. You should see the ball move to the right more slowly. However, it keeps on going right through the wall, off into empty space, because this is what it was told to do. VPython doesn't know any physics! You have to tell it what to do.

IMPORTANT: An animation loop must contain a rate statement (or sleep or waitfor statement). Otherwise the browser page will lock up with no possibility of updating the page.

Making the ball bounce: Logical tests

To make the ball bounce off the wall, we need to detect a collision between the ball and the wall. A simple approach is to compare the x coordinate of the ball to the x coordinate of the wall, and reverse the x component of the ball's velocity if the ball has moved too far to the right. In VPython you can access the x , y , or z component of any vector by referring to the `x`, `y`, or `z` attribute of that vector. In the statements below, `ball.pos` is a vector, and `ball.pos.x` is the x component of that vector. Similarly, `ball.velocity` is a vector, and `ball.velocity.x` is the x component of that vector.

Insert these statements into your while loop, just before your position update statement (press  at the end of the preceding statement, or insert tabs before the new statements, or select both lines and press ):

```
if ball.pos.x > wallR.pos.x:
    ball.velocity.x = -ball.velocity.x
```

The indented statement after the if statement will be executed (and reverse the x component of velocity) only if the logical test in the previous line gives True for the comparison. If the result of the logical test is False (that is, if the x coordinate of the ball is not greater than the x coordinate of the wall), the indented line will be skipped. We want this logical test to be performed every time the ball is moved, so we need to indent both of these lines, so they are inside the while loop.

This section of your code should now look like this:

```
while t < 3:
    rate(100)
    if ball.pos.x > wallR.pos.x:
        ball.velocity.x = -ball.velocity.x
    ball.pos = ball.pos + ball.velocity*deltat
    t = t + deltat
```

You should observe that the ball moves to the right, bounces off the wall, and then moves to the left, continuing off into space. Note that our test is not very sophisticated; because `ball.pos.x` is at the center of the ball and `wallR.pos.x` is at the center of the wall, if you look closely you can see that the ball appears to penetrate the wall slightly. You could if you wish make the test more precise by using the radius of the ball and the thickness of the wall.

Add another wall at the left side of the display, and give it the name `wallL`. Make the ball bounce off that wall also. You need to create a left wall near the beginning of the program, before the while loop. If you put the statement inside the loop, a new wall would be created every time the loop was executed. A very large number of walls would be created, all at the same location. While we wouldn't be able to see them, the computer would try to draw them, and this would slow the program down considerably.

Next, before the while loop, change the initial velocity to have a nonzero y component.

```
ball.velocity = vector(25,5,0)
```

When you run the program, the ball bounces even where there is no wall! Again, the issue is that VPython doesn't know any physics.

If we tell it to make the ball change direction when the ball's position is to the right of the wall's position, VPython goes ahead and does that, whether that makes physics sense or not. We'll fix this later.

Visualizing velocity

We will often want to visualize vector quantities, such as the ball's velocity. We can use an arrow object to visualize the velocity of the ball.

Before the while loop, but after the program statement that sets the ball's velocity, create an arrow, which you will use to visualize the velocity vector for the ball. The tail of the arrow is at the location given by `pos`, and we choose that to be the location of the ball. The tip of the arrow is at the location that is a vector displacement away from the tip (in this case, the location of the ball plus the velocity of the ball).

```
varr = arrow(pos=ball.pos, axis=ball.velocity, color=color.yellow)
```

It is important to create the arrow before the while loop. If we put this statement in the indented code after the while, we would create a new arrow in every iteration. We would soon have a large number of arrows, all at the same location. This would make the program run very slowly.

Run your program. You should see a yellow arrow with its tail located at the ball's initial position, pointing in the direction of the ball's initial velocity. However, the arrow is huge, and it completely dominates the scene. The problem is that velocity in meters per second and position in meters are basically different kinds of quantities, and we need to scale the velocity in order to fit it into the diagram.

Let's scale down the size of the arrow, by multiplying by a 'scalar', a single number. Multiplying a scalar times a vector changes the magnitude of a vector but not its direction, since all components are scaled equally.

Change your arrow statement to use a scale factor to scale the axis, like this, then run the program:

```
vscale = 0.1  
varr = arrow(pos=ball.pos, axis=vscale*ball.velocity, color=color.yellow)
```

Run the program. Now the arrow has a reasonable size, but it doesn't change when the ball moves. We need to update the position and axis of the arrow every time we move the ball.

Inside the while loop, update the position and axis attributes of the arrow named `varr`, so that the tail of the arrow is always on the ball, and the axis of the arrow represents the current vector velocity. Remember to use the scale factor `vscale` to scale the axis of the arrow. Run the program.

The arrow representing the ball's velocity should move with the ball, and should change direction every time the ball collides with a wall.

Autoscaling

By default, VPython 'autoscales' the scene, by continually moving the camera forwards or backwards so that all of the scene is in view. If desired, you can turn off autoscaling after creating the initial scene.

Just before the while loop, after drawing the initial scene, turn off further autoscaling:

```
scene.autoscale = False
```

Leaving a trail

Often we are interested in the trajectory of a moving object, and would like to have it leave a trail. This can be done simply when creating the ball by specifying that `make_trail` be true:

```
ball = sphere(pos=vector(-5,0,0), radius=0.5,  
color=color.cyan, make_trail=True)
```

How your program works

In your while loop you continually change the position of the ball (`ball.pos`); you could also have changed its colour or its radius. The `rate(100)` statement not only pauses as necessary to limit the animation speed to 100 iterations per second but also causes the scene to be redisplayed ('rendered') about 60 times per second, with the current positions of the objects. With the scene rendered so often, the animation looks continuous.

Making the ball bounce around inside a box

With the program you've written so far, the ball escapes and bounces off nothing. To make a more realistic model of the motion, do the following:

- Add top and bottom walls, and make the ball bounce off these walls.
- Make the walls touch, forming part of a large box.
- Add a back wall, and an "invisible" front wall, and make the ball bounce off these walls. Do not draw a front wall, but include an if statement to prevent the ball from coming through the front.
- Give your ball a component of velocity in the z direction as well, so that it will bounce off the back and front walls. Make the initial velocity of the ball be this:

```
ball.velocity = vector(25,5,15)
```

The completed program should include these features:

- Complete box (except that the front is open).
- Correct initial velocity.
- Continuous display of velocity arrow that moves with the ball.
- Ball leaves a trail.

It is worth pointing out that this program represents a simple model of a gas in a container. The pressure on the walls of the container is due to the impacts of large numbers of gas molecules hitting the walls every second.

Playing around

Here are some suggestions of things you might like to play with after completing your program.

- You can make the program run much longer by changing to `while t < 3e4`: or you can make it run 'forever' by changing to `while True`: since the condition is always True.
- You might like to add some more balls, with different initial positions and initial velocities. Inside the loop you will need position updates for each ball.

- You could make a ‘Pong’ game by moving walls around under mouse control. See the sections on Mouse Events in the VPython Help.
- You can design your own colors using fractional values for the amount of red, green, and blue. For example, if you specify `color=vector(1, 0.7, 0.7)` you get a kind of pink (100% red, 70% green, 70% blue). The example program Color-RGB-HSV lets you experiment with colors.
- You could change the color of the ball or the wall whenever there is a collision.



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